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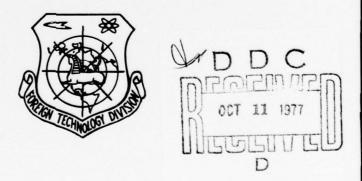




INVESTIGATION OF VELOCITY FIELD BEHIND LOW-FLYING WING WITH FUSELAGE

by

M. K. Bochin, L. G. Tsvetkov



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Block	Italic	Transliteration	Block	Italic	Transliteration
Аа	A a	A, a	Pр	Pp	R, r
Бб	Бб	B, b	Сс	Cc	S, s
Вв	B &	V, v	Тт	T m	T, t
Гг	Γ :	G, g	Уу	у у	U, u
Дд	Д д	D, d	ФФ	Φφ	F, f
Еe	E .	Ye, ye; E, e*	X×	X x	Kh, kh
Ж ж	жж	Zh, zh	Цц	4	Ts, ts
З з	3 3	Z, z	4 4	4 4	Ch, ch
Ии	н и	I, i	Шш	Шш	Sh, sh
Йй	A I	Ү, у	Щщ	Щщ	Sheh, sheh
Нн	KK	K, k	Ъъ	ъ .	"
	ЛА	L, 1	ы	ы	Ү, у
	Мм	M, m	Ьь	ь ь	•
Нн	Н ж	N, n	Ээ	9 ,	Е, е
0 0	0 0	0, 0	н н	Юю	Yu, yu
n n	Пп	P, p	Яя	Яя	Ya, ya

*ye initially, after vowels, and after ъ, ь; e elsewhere. When written as ë in Russian, transliterate as yë or ë. The use of diacritical marks is preferred, but such marks may be omitted when expediency dictates.

GREEK ALPHABET

A	α	Q		Nu	N	V	
В	β			Xi	Ξ	ξ	
Γ	Υ			Omicron	0	0	
Δ	δ			Pi .	П	Π	
Ε	ε	•		Rho	P	ρ	6
Z	5			Sigma	Σ	σ	ς
Н	n			Tau	T	τ	
Θ	θ	9		Upsilon	T	υ	
I	ι			Phi	Φ	φ	Φ
K	n	K	×	Chi	Х	χ	
Λ	λ			Psi	Ψ	ψ	
М	μ			Omega	Ω		
	Γ Δ E Z H Θ I K	B β Γ γ Δ δ Ε ε Z ζ Η η Θ θ I ι Κ χ Λ λ	B β Γ γ Δ δ Ε ε ε Ε Σ ζ Η η Θ θ \$ Ι ι Κ χ Κ Λ λ	B β Γ γ Δ δ Ε ε ε Ζ ζ Η η Θ θ \$ Ι ι Κ κ κ κ	B β Xi Γ γ Omicron Δ δ Pi E ε ε Rho Z ζ Sigma H η Tau Θ θ \$ Upsilon I ι Phi K κ κ Chi Λ λ Psi	B $β$ Xi E $Γ$ $γ$ $Omicron$ O $Λ$ $δ$ Pi $Π$ E $ε$ $ε$ Rho P Z $ζ$ $Sigma$ $Σ$ H $η$ Tau T $Θ$ $θ$ $$$Upsilon$ T I	B B Xi E ξ Γ γ Omicron O o Δ δ Pi Π Π E ε Rho P ρ Z ζ Sigma Σ σ H η Tau T τ Θ Θ \bullet Upsilon T \cup I ι Phi Φ Φ K \bullet K \bullet Chi \bullet X \bullet Λ λ Psi Ψ ψ

RUSSIAN AND ENGLISH TRIGONOMETRIC FUNCTIONS

Russ	ian	English
sin		sin
cos		cos
tg		tan
ctg		cot
sec		sec
cose	С	csc
sh		sinh
ch		cosh
th		tanh
cth		coth
sch		sech
csch	1	csch
arc	sin	sin ⁻¹
arc	cos	cos-l
arc	tg	tan-1
arc	ctg	cot-1
arc	sec	sec-1
arc	cosec	csc ⁻¹
arc	sh	sinh-1
arc	ch	cosh-1
arc	th	tanh-1
arc	cth	coth-1
arc	sch	sech-1
arc	csch	csch-l
	_	
rot		curl
lg		log

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INVESTIGATION OF VELOCITY FIELD BEHIND LOW-FLYING WING WITH FUSELAGE

(Presented at Scientific and Technical Conference of Lenin Ship Euilding Institute (LKI), October 1969)

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In this article we propose a method of investigating the velocity field behind a low-flying wing with fuselage. The value of the velocity field is necessary in calculating the aerodynamic characteristics of the tail assembly of aircraft which use the screen effect.

Numerical Calculation Method of Velocity Field

We investigate the uniform movement of a wing of finite span with a fuselage above a solid screen. The sheet of solid vortices which is formed twist, according to [1], into two vortex tip filaments, which lie upstream from the wing. The intensity and arrangement of the vortices are determined in the main velocity field behind the wing. Therefore, in our study we will ignore the stream caused by the attached wing vortex. Coordinate system Ox'y'z', attached to the wing (Fig. 1), is selected such that the attached vortex of the supporting wing lies within plane y'oz': the ox' axis lies downstream from the fuselage; the cy' axis vertically above it. The fuselage is assumed to have the shape of a circular finite cylinder with a zero angle of attack. Cur symbols are: uo - velocity of undisturbed oncoming flow parallel to ox' axis and plane of screen; T+ - intensity of vortex tip filaments; \(\bullet - \) their distance from diametrical plane; e - elevation of free vortices above fuselage axis; h - distance of fuselage axis from screen; R - radius of cylindrical fuselage. Work [3] should be used as a guide in selecting the arrangement of the free vortex filaments.

In order to satisfy the condition of nonleakage on the fuselage from vortices 1 and 2 (Fig. 1) in the case of a wing and fuselage moving in an infinite fluid, according to [2] we place vortices 3 and 4 at the points of inversion inside the fuselage. In order to satisfy the boundary condition of nonpenetration in the case of a system moving near a solid screen, we map on it in mirror image relative to the plane of the screen the preceding vortex system, thus obtaining a hypothetical vortex system (vortices 5-8). In order to eliminate the viclated condition of nonpenetration on the fuselage while preserving it on the screen, we use the method of successive inversion of vortices, in which each vortex of the hypothetical system (vortex Aq. Fig. 2) is mapped in relation to the surface of the fuselage, placing at the point of inversion vortex B_1 , which is mapped relative to the screen - vortex A1. Then, we perform a second approximation - vortex A; is mapped on B2 and E2 - on A2, etc. As a result of this chains of vortices are formed inside the main and hypothetical fuselages, and in the presence of vortex A*o, which is symmetrical relative the diametric plane of vortex Ao, the same chains are formed, although this time symmetrical in relation to M with circulation of the crposite sign. After the γ-order of approximation the "residual leakage" of the fuselage is the result of vortices Ar and Ar, which, as the approximation order increases, move closer together, reducing the velocities induced by them and thus assuring necessary accuracy in satisfying the boundary condition on the fuselage. The complete

vortex system corresponding to the studied problem is shown in Fig.
1, where dashed lines represent the chains of vortices.

Let us determine vertical downwash $\mathbf{w} = \frac{\hat{\mathbf{v}}_{E}}{\mathbf{u}_{o}}$ at point M(x*, y*, z*), after introducing the dimensionless quantity

$$\Gamma = \frac{\Gamma_{+}}{u_{o}\ell}; \quad \overline{R} = \frac{R}{\ell}; \quad \overline{e} = \frac{e}{\ell}; \quad \overline{h} = \frac{h}{\ell}; \quad \alpha = \frac{\alpha'}{\ell}; \quad \xi = \frac{\xi'}{\ell} \text{ etc.}$$
 (1)

After applying the Biot-Savart formula to the elements of the vortex system of Fig. 1, we get:

$$\mathbf{w} = \frac{\Gamma}{4\pi} \left[\sum_{n=1}^{8} (-1)^{n+1} \cdot \frac{\mathbf{x} - \zeta_n}{\tau_n^2} \left(1 + \frac{\mathbf{x}}{\sqrt{\mathbf{x}^2 + \tau_n^2}} \right) + \sum_{j=1}^{8} \sum_{k=1}^{8} (-1)^{k} \cdot \frac{\mathbf{x} - \zeta_k^2}{(\tau_k^2)^2} \left(1 + \frac{\mathbf{x}}{\sqrt{\mathbf{x}^2 - (\tau_k^2)^2}} \right) \right], \tag{2}$$

where

$$\tau_n = \sqrt{(z - \zeta_n)^2 + (y - \gamma_n)^2}; \quad \tau_k = \sqrt{(z - \zeta_k) + (y - \gamma_k)^2}; \quad (3)$$

 γ_n and ζ_n are the coordinates of vortices 1-8, where n is the number of the vortex according to Fig. 1.

The values of the coordinates have the form of

$$\zeta_{1} = \zeta_{6} = -\zeta_{2} = -\zeta_{5} = 1; \quad \zeta_{4} = \zeta_{7} = -\zeta_{5} = -\zeta_{8} = \frac{\overline{R}^{2}}{1 + \overline{e}^{2}}; \quad \gamma_{1} = \gamma_{2} = \overline{e}$$

$$\gamma_{5} = \gamma_{4} = \overline{e} \frac{\overline{R}^{2}}{1 + \overline{e}^{2}}; \quad \gamma_{5} = \gamma_{6} = -(2\overline{h} + \overline{e}); \quad \gamma_{7} = \gamma_{6} = -\left(2\overline{h} + \overline{e} \frac{\overline{R}^{2}}{1 + \overline{e}^{2}}\right)$$
(4)

 η_A^{γ} and η_A^{γ} are the coordinates of the vortices in the chain, where λ is the number of the chain (according to Fig. 1): γ - the number of the vortex in the chain (or order of approximation).

The coordinates of the vortices in the chains in shifting from approximation γ to approximation $\gamma + 1$ when $\lambda = 6$ and $\lambda = 7$ are calculated according to the formulas:

$$\zeta_{\lambda}^{t+1} = \frac{\bar{R}^{2} \cdot \zeta_{\lambda}^{t}}{(\zeta_{\lambda}^{t})^{2} + (2\bar{h} + \gamma_{\lambda}^{t})^{2}}; \qquad \gamma_{\lambda}^{t+1} = -\frac{\bar{R}^{2}(2\bar{h} + \gamma_{\lambda}^{t})}{(\zeta_{\lambda}^{t})^{2} + (2\bar{h} + \gamma_{\lambda}^{t})^{2}}. \tag{5}$$

Then, the coordinates of the vortices in the chains for the given order of approximation (γ = const) are related to ζ_6^r ; ζ_7^r ; ζ_6^r and ζ_7^r by relationships:

The coordinates of the first vortices in the chains ($\gamma=1$) when $\lambda=6$ and $\lambda=7$ are determined by formulas (5) through coordinates with corresponding indices n=6 and n=7, which are calculated according to formula (4).

By using the Bernoulli equation and applying the Biot-Savart formula to the elements of the vortex system of Fig. 1, we get a formula for calculating the distribution of the pressure coefficient over the surface of a cylindrical fuselage:

$$\overline{p} = \frac{\Gamma^2}{16\pi^2} \left[\sum_{n=1}^8 (1)^{n+1} \frac{\overline{k} - \zeta_n \cos\theta - \gamma_n \sin\theta}{\rho_n^2} \left(1 + \frac{x}{\sqrt{x^2 - \rho_n^2}} \right) + \sum_{\gamma=1}^8 \sum_{A=1}^8 (-1)^{A} \frac{\overline{k} - \zeta_A^{\gamma} \cos\theta - \gamma_A^{\gamma} \sin\theta}{\left(\rho_A^{\gamma} \right)^2} \left(1 + \frac{x}{\sqrt{x^2 + (\rho_A^{\gamma})^2}} \right) \right]^2, \quad (7)$$

where

$$\rho_n = \sqrt{(\bar{R}\cos\theta - \zeta_n)^2 + (\bar{R}\sin\theta - \zeta_n)^2}; \qquad \rho_A^{I} = \sqrt{(\bar{R}\cos\theta - \zeta_A^{I}) + (\bar{R}\sin\theta - \zeta_A^{I})^2}; \tag{8}$$

6 - is the polar angle of the studied point on the fuselage surface, reckoned from the horizontal plane.

In calculating quantities \mathbf{w} and \mathbf{p} according to formulas (2) and (7) we should limit ourselves to approximation $\gamma \approx k$, where the increment in the sum with respect to γ becomes lower than the required accuracy of calculating quantities \mathbf{w} or \mathbf{p} .

According to this method a calculation was performed for a section of infinite distance downstream for the distribution of the reduced coefficient of pressure $\frac{F}{\Gamma^2}$ over the surface of the fuselage

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(Fig. 3) and the reduced vertical downwash $\frac{w}{\Gamma}$ along the wing span (Fig. 4) for the following calculated parameters: $\overline{R} = \frac{R}{\ell} = 0.20; \ \overline{h} = \frac{h}{\ell} = 0.25; \ \overline{e} = 0.$

Investigation of Velocity Field on EGDA Device

For a section of infinite distance along the stream the investigation of the velocity field behind a low-flying wing with a cylindrical fuselage can be done on a plane electrohydrodynamic analogy device [the EGDA], as shown in Fig. 5.

The symbols in Fig. 5: 1 - sheet of electroconductive paper, 2 - tus, 3 - electrode which simulates vortex, 4 - sheet of electroconductive paper which simulates plane undisturbed flow, 5 - direct current source, 6 - galvanometer, 7 - probe.

Simulation of the free vortex flowing cff cf the wing tip is done by an electrode (source of electrical field). Observance of the boundary conditions requires that the contour (cf fuselage and screen) in this analogy be made from a conductor. The symmetry of the flow in relation to the diametric plane is assured by installing a bus in this plane. In this case the force lines of the electrical field will correspond to the equipotential lines in the stream of

fluid, the equipotential lines of the electrical field - to the flow lines in the fluid.

The posed problem for a section of infinite length was modeled on the EGDA. The following was obtained: the field of vertical downwashes over the span of the wing (compared with calculations on Fig. 4), field of vertical downwashes at location of tail assembly (Fig. 6), and pattern of flow lines (Fig. 7) for following parameters: $\bar{R} = 0.20$; $\bar{h} = 0.25$ and $\bar{e} = 0.25$

conclusions

1. The experiments performed on the electrohydrodynamic analogy device verified the proposed method for calculating the velocity field behind a low-flying wing with cylindrical fuselage both qualitatively and quantitatively.

- 2. The cylindrical fuselage substantially affects the velccity field near the fuselage, within a region of 2-2.5 times its radius, decreasing or increasing the vertical downwash depending on the location of the studied point.
- 3. When the system of wing and fuselage approach the screen, the rarefaction curve on the surface of the fuselage, which is caused by the vertex sheet flowing cff of the wing, decreases on one hand,

while on the other there occurs a redistribution in this curve, as a result of which additional lifting force develops on the fuselage.

This deduction must also qualitatively be verified by the pattern of flow lines obtained on the EGDA.

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Fig. 1.

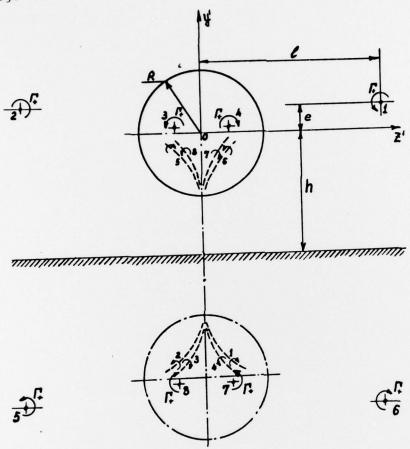


Fig. 2.

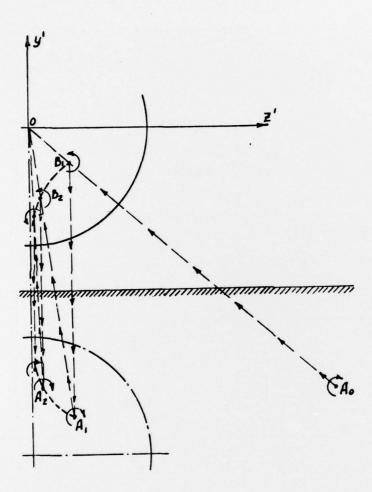


Fig. 3.

(1) Macumes 1/2 0 4000 4010

Key: (1) Scale p/g2.

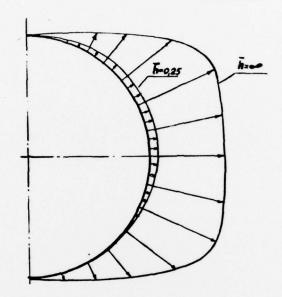
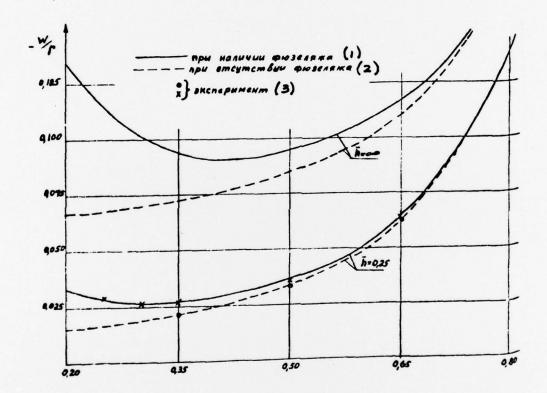


Fig. 4.

Key: (1) with fuselage, (2) without fuselage, (3) experiment.



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Fig. 5.

Key: (1) Screen.

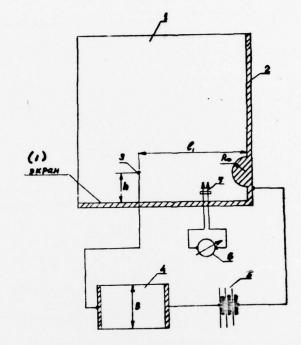


Fig. 6.

Key: (1) without fuselage, (2) with fuselage.

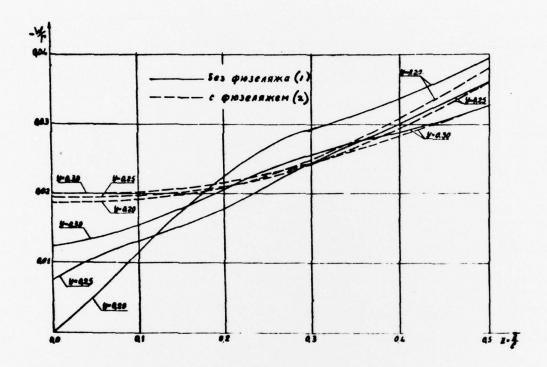
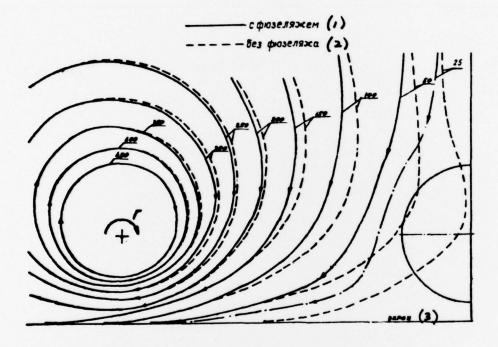


Fig. 7.

Key: (1) without fuselage, (2) with fuselage, (3) screen.



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